

Modeling coupled water and heat transport in a freezing soil using the modified HYDRUS-1D code.

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Liquid water & ice coexist in a frozen soil (Unfrozen water, θ_u)

Soil freezing model

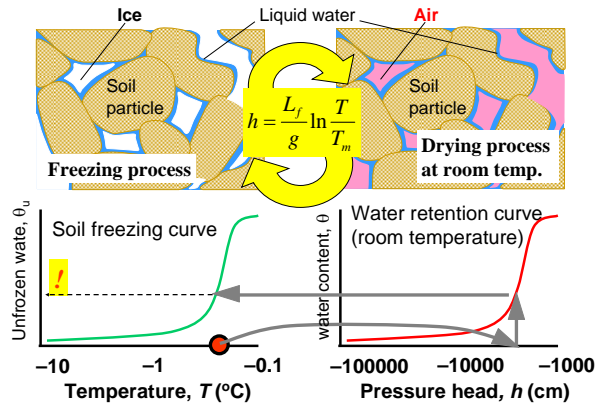
Water

$$\frac{\partial \theta_u}{\partial t} + \frac{\rho_i}{\rho_w} \frac{\partial \theta_i}{\partial t} = \frac{\partial}{\partial z} \left[K_{lh}(h) \frac{\partial h}{\partial z} + K_{lv}(h) \frac{\partial T}{\partial z} + K_{lw}(h) \frac{\partial h}{\partial z} + K_{wt}(\theta) \frac{\partial T}{\partial z} \right]$$

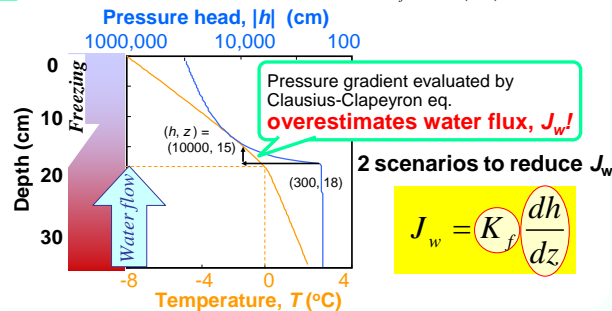
Heat

$$\frac{\partial C_p T}{\partial t} - L_f \rho_i \frac{\partial \theta_i}{\partial t} + L_v(T) \frac{\partial \theta_i}{\partial t} = \frac{\partial}{\partial z} \left[\lambda(\theta) \frac{\partial T}{\partial z} \right] - C_{un} \frac{\partial q_{un} T}{\partial z} - C_v \frac{\partial q_v T}{\partial z} - L_v(T) \frac{\partial q_v}{\partial z}$$

Pressure of θ_u in frozen soil is related to temperature with the Clausius-Clapeyron equation (C-C eq.).



Calculating soil freezing using $K_f = K(\theta_u)$



Two possible scenarios for the reduce of J_w

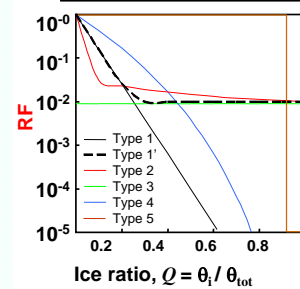
Scenario 1: Reduce hydraulic conductivity of the frozen soil

The reduction function, RF for K

$$K_f = RF \times K = 10^{-\Omega Q} \times K$$

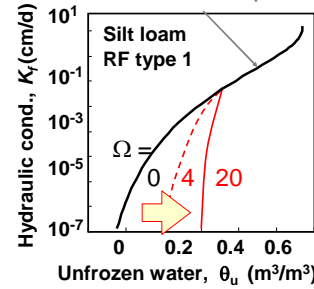
List of example formula for RF

- Type 1 $10^{-\Omega Q}$ Type 3 $10^{-\Omega}$
- Type 1' Cut off Type 4 $(1-Q)^\Omega$
- Type 2 $10^{-\Omega Q^\alpha}$ Type 5 Step

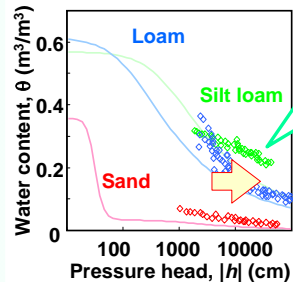


K : hydraulic cond. at room temperature
 K_f : hydraulic cond. of frozen soil
 Q : ice to total water ratio
 Ω : impedance factor

VG-Mualem eq.



Scenario 2: Modify h - T relationship (Clausius-Clapeyron eq.)



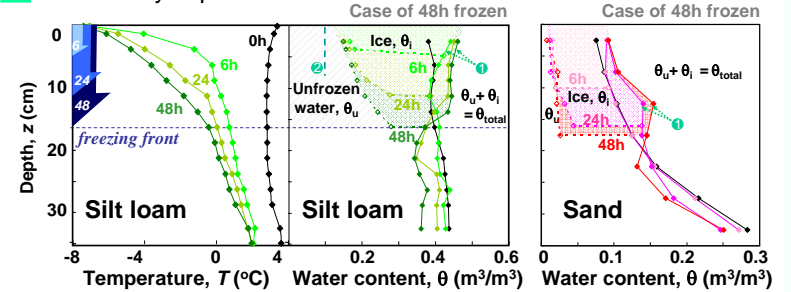
During soil freezing,
 Freezing θ_u exp. > Observed θ_u VG eq.
 (due to the ice formation time)

Apparent h would be given as

$$h = RF \frac{L_f}{g} \ln \frac{T}{T_m}$$

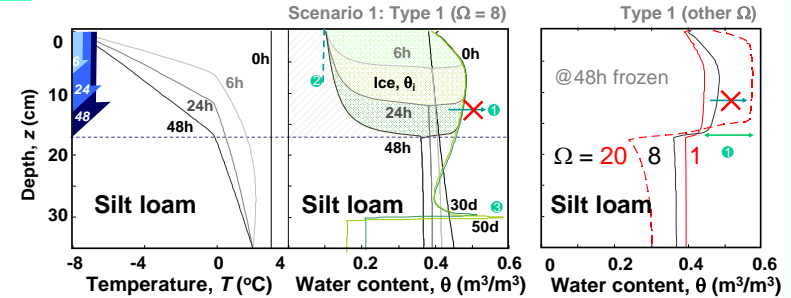
ex. RF = const.
 $= \theta_{total} / \theta_s$

Laboratory experiment



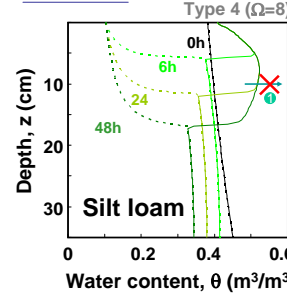
- $h, T, \theta_u, \theta_{total}$ profiles were measured for 3 freezing soils with various θ_{init}
- θ_{total} in frozen regions of silt loam and sand increased with time (ice kept growing).

HYDRUS calculation

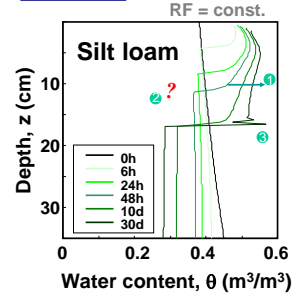


- Ω could change the θ_{total} , but could not describe the ice growth in frozen regions.
- θ_u was slightly underestimated compared to laboratory experiments.
- A sharp peak was observed at the freezing front at long-time, due to the underestimation of K_f .

Scenario 1



Scenario 2



- Formula type of RF is not sensitive to J_w in frozen regions (Scenario 1).
- Modified C-C eq. improved the ice growth in frozen regions (Scenario 2).
- θ_u was overestimated and the soil froze only shallow depth (Scenario 2).